



Wrocław University of Technology

**Application of an evolution algorithm and
cluster computing for parameters
identification of the
Friderick-Armstrong's material model**

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Introduction

Internal parameters

Processes observed in cyclicly loaded material could be modelled by internal parameters introduced into constitutive relation. Following parameters could be distinguished:

- ▶ kinematic hardening,
- ▶ isotropic hardening,
- ▶ damage parameter and others.

Therefore constitutive relation becomes differential or integral equation, very often without a solution as an elementary function.



Material model

General assumptions

- ▶ elastic-plastic material model with Frederick-Armstrong's kinematic hardening parameter,
- ▶ Hubera-Mises yield condition:

$$\sqrt{(s - X)(s - X)} - R = 0, \quad (1)$$

where s - stress tensor deviator, X - back stress, R - yield point.



Material model

Constitutive equation

Applying appropriate evolution equation one may achieve

$$\dot{X}_{ij} = C^{(k)} \dot{\varepsilon}_{ij}^p - \gamma^{(k)} \dot{\lambda} X_{ij}^{(k)}, \quad (2)$$

where $\dot{\lambda} = \sqrt{\frac{2}{3} \dot{\varepsilon}_{ij}^p \dot{\varepsilon}_{ij}^p}$ - change of plastic strain trajectory,
 $C^{(k)}$ i $\gamma^{(k)}$ - parameter that may be functions of internal
variables, ε_{ij}^p - plastic strain tensor.



Material model

Constitutive equation

In 1D case, for one plasticity surface ($k = 1$) and linear Frederick-Armstrong's evolution equation:

$$\dot{X} = C\dot{\varepsilon}_p - \gamma|\dot{\varepsilon}_p|X \quad (3)$$

and

$$\sigma = X \pm R. \quad (4)$$

For constant C i γ equation (3) is a linear equation with a solution as an elementary function

$$\sigma = \left(R - \sigma_a - \frac{C}{\gamma}\right)e^{-\gamma(\varepsilon_p + \varepsilon_{ap})} + \frac{C}{\gamma}. \quad (5)$$



Material model

Constitutive equation

If the γ is a function of plastic strain trajectory

$$\gamma = \gamma(\lambda), \quad \lambda = \int_0^t |\dot{\epsilon}_p| dt. \quad (6)$$

$$\dot{X} = C\dot{\epsilon}_p - \gamma(\lambda)|\dot{\epsilon}_p|X \quad (7)$$



Experiment

- ▶ austenitic steel AISI 304 ($E = 1,93e5[MPa]$),
- ▶ material exhibit strong hardening under cyclic loads,
- ▶ round specimen,
- ▶ material test system by MTS company,
- ▶ load - constant amplitude total strain signal.



Experiment

Modelling material cyclic hardening implies taking:

- ▶ variable yield point R ,
- ▶ variable relaxation parameter γ .

Second option was selected because parameter γ defines relaxation that decreases due to increase of martensitic phase.



Identification procedures

Identification criterion

Following identification criterion was assumed

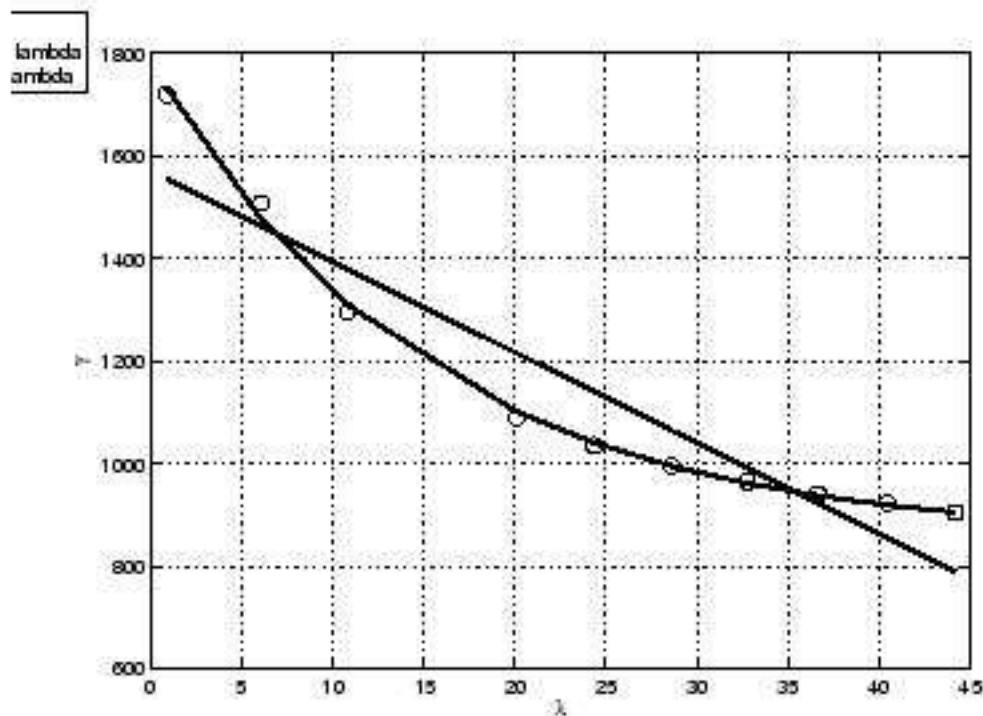
$$Q = \sum_{i=0}^N (\sigma(t_i) - \tilde{\sigma}(t_i))^2 \quad (8)$$

where $\sigma(t_i)$ - measured material response (stress signal),
 $\tilde{\sigma} = \tilde{\sigma}(t_i; \mathbf{C}, R, X_0, \gamma(\lambda(t_i)))$ - computed material response.



Identification procedures

Function $\gamma(\lambda)$





Identification procedures

Function $\gamma(\lambda)$

Relaxation function

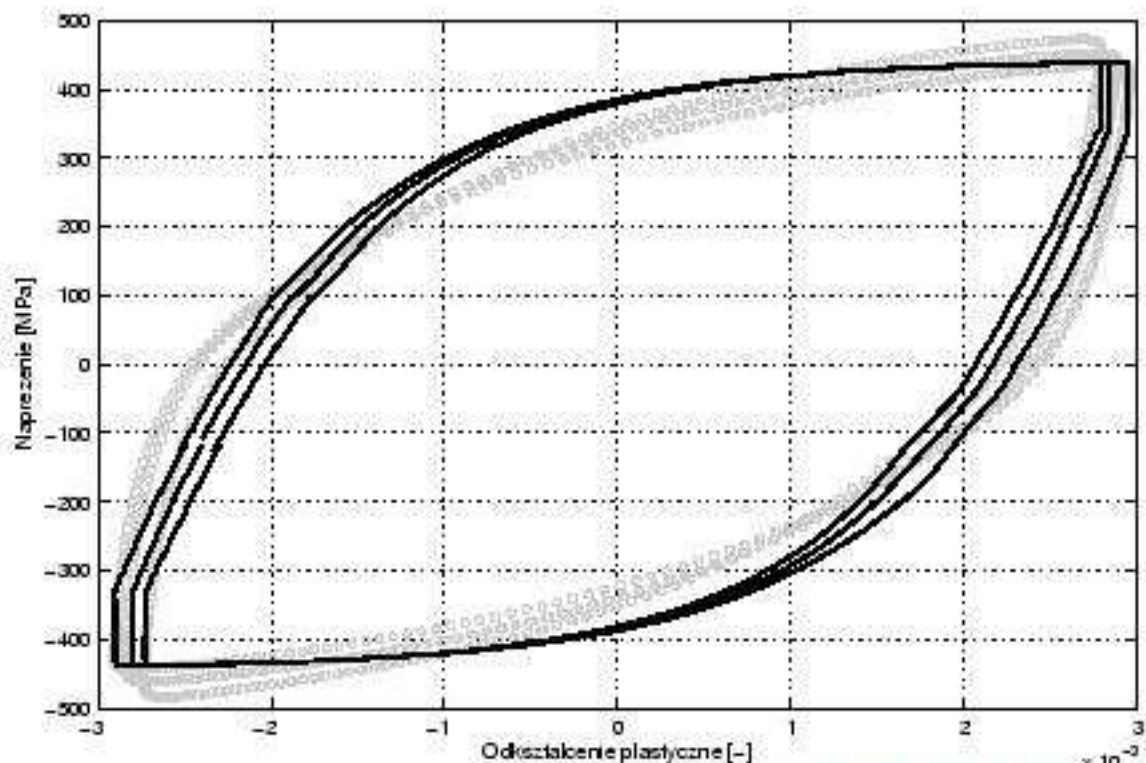
$$\gamma(\lambda) = e^{a\lambda+b} + c \quad (9)$$

was selected and therefore identification parameters vector takes following form $x_i = [C, R, X_0, a, b, c]$.



Identification procedures

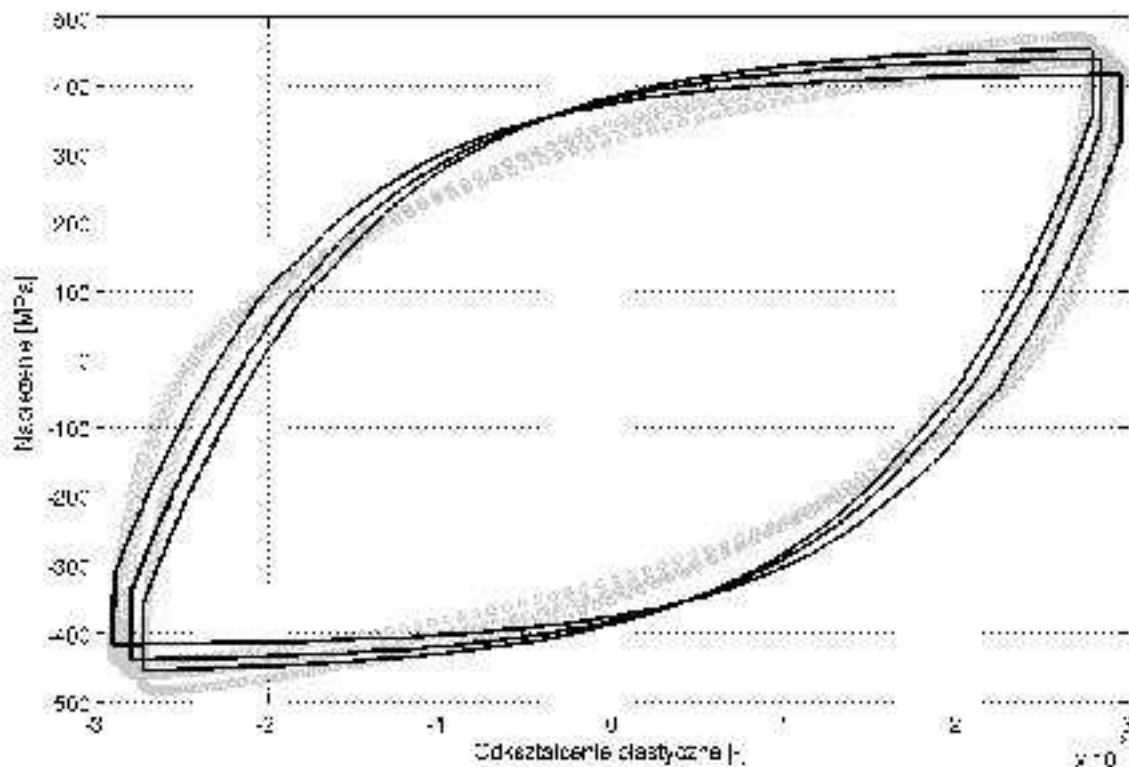
Typical plots for constant γ





Identification procedures

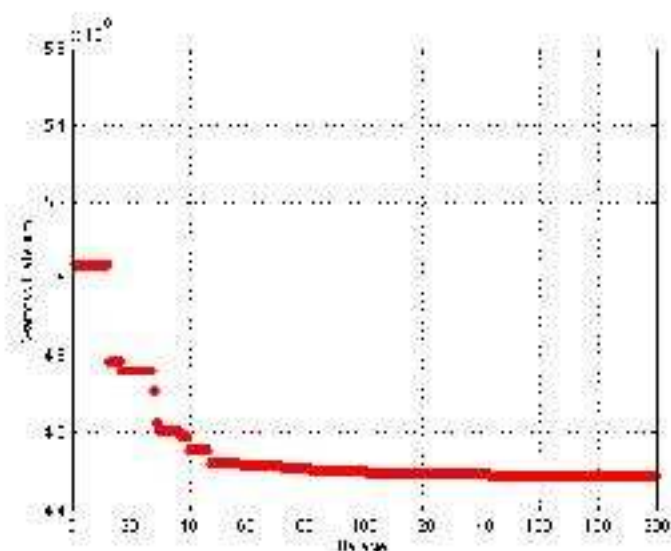
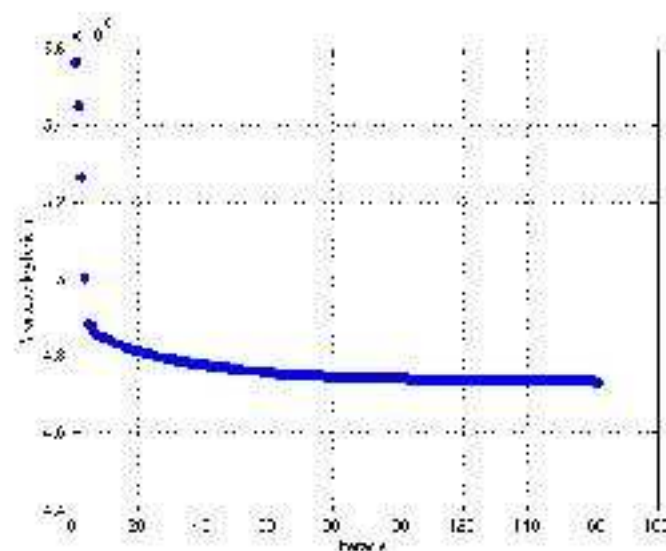
Typical plots for variable γ





Identification procedures

Typical plots of criterion value changes



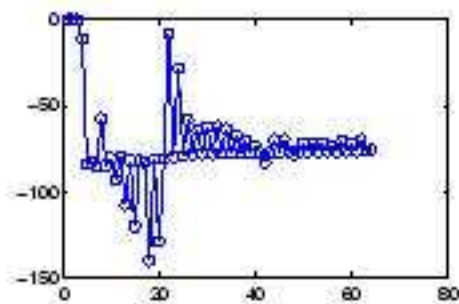
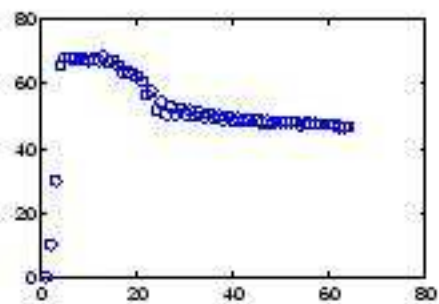
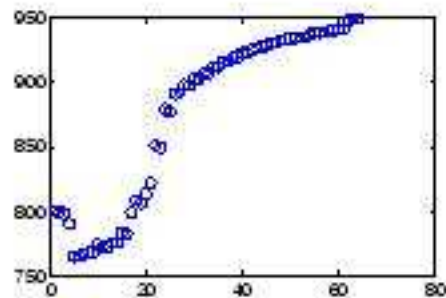
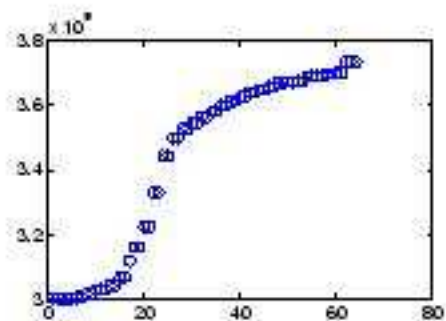
$$X_{CG} = [377079; 49; -324; -0,067; 6,92; 874]$$

$$X_{DE} = [431892; 38; -193; -0.062; 7.02; 971]$$



Identification procedures

Typical plots of identified parameters' values changes





Behind the scenes

Differential evolution algorithm

- ▶ One of the world fastest optimisation algorithm.
- ▶ Developed by Price & Storn for Chebyshev Polynomial fitting problem in 1995.
- ▶ Since that applied in many fields like:
 - ▶ digital filter design,
 - ▶ neural networks learning,
 - ▶ electricity market simulation,
 - ▶ wide range of optimisation problems.



Behind the scenes

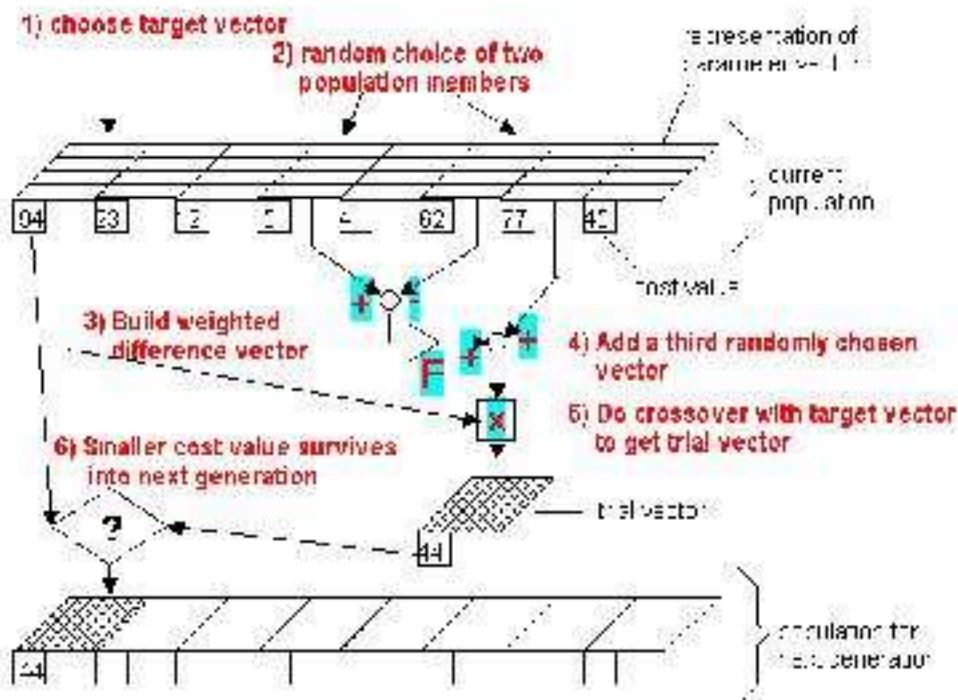
Differential evolution algorithm outline

- ▶ random choice of initial population of parameter vectors from defined range,
- ▶ computation criterion value for each vector,
- ▶ cross, according to selected strategy, two vectors and generate third one,
- ▶ build second generation of parameter vectors.



Behind the scenes

Differential evolution algorithm outline





Behind the scenes

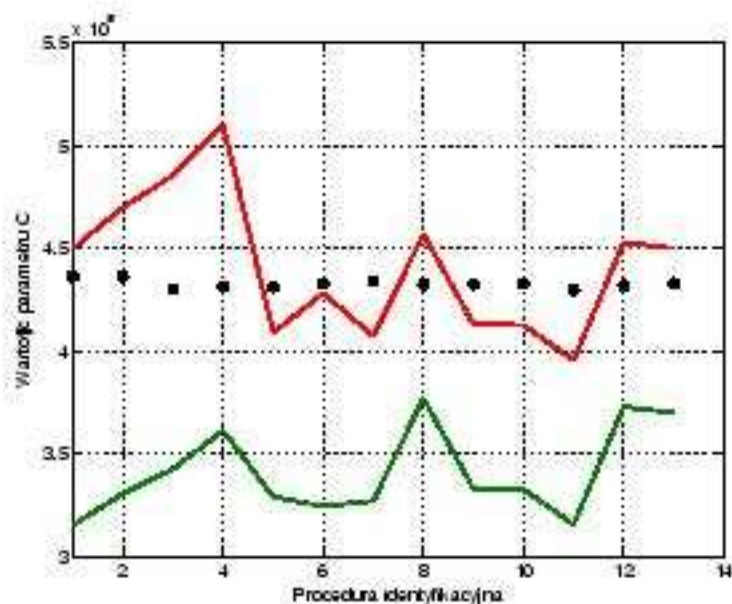
Example of cluster application

- ▶ 13 nodes were used,
- ▶ 13 ranges for initial vector parameters population were randomly chosen,
- ▶ 13 values for every parameter were computed in time needed for computation of 1 value on a single computer.



Behind the scenes

Example of cluster application

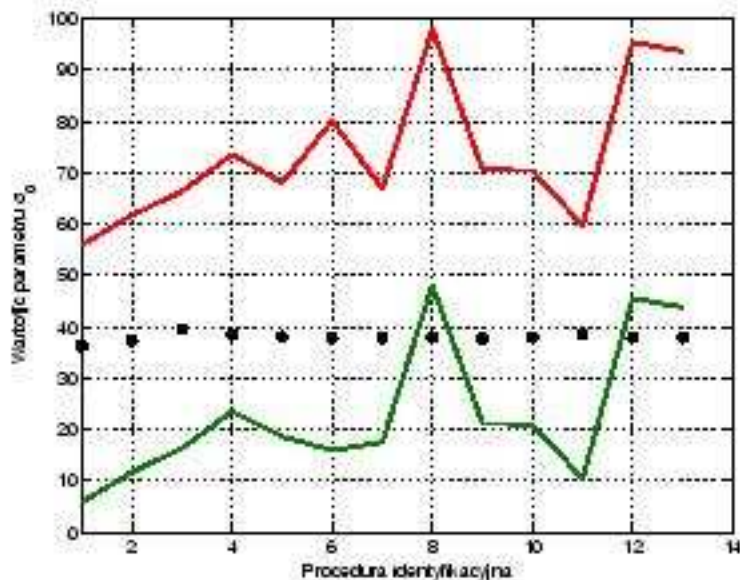


Parameter C obtained on cluster nodes and initial vector parameter range



Behind the scenes

Example of cluster application

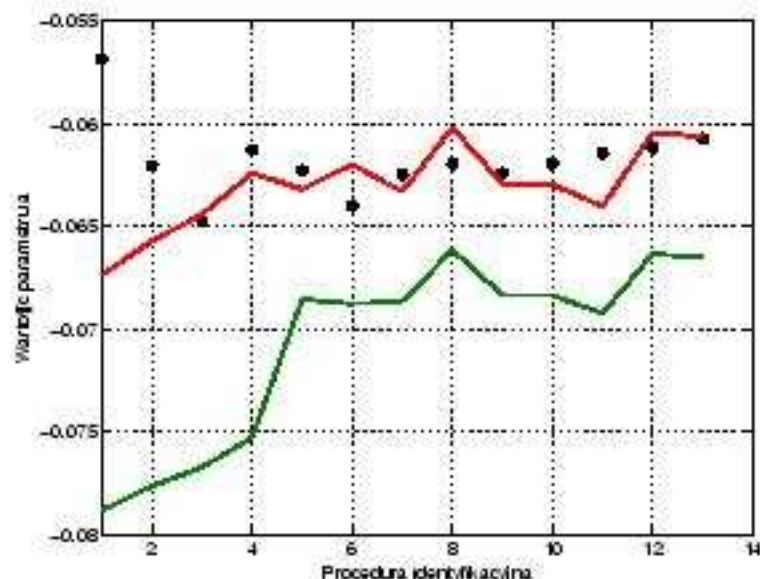


Yield point R value obtained on the cluster nodes and initial vector parameter range



Behind the scenes

Example of cluster application

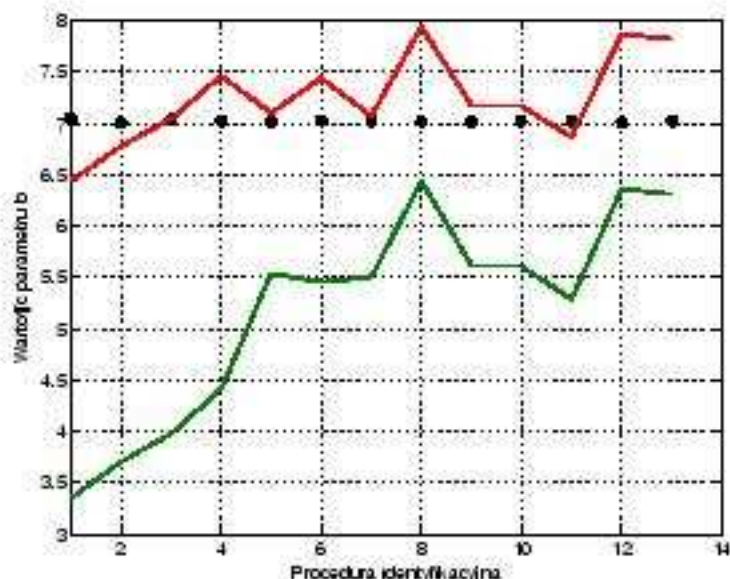


Parameter a obtained on the cluster nodes and initial vector parameter range



Behind the scenes

Example of cluster application

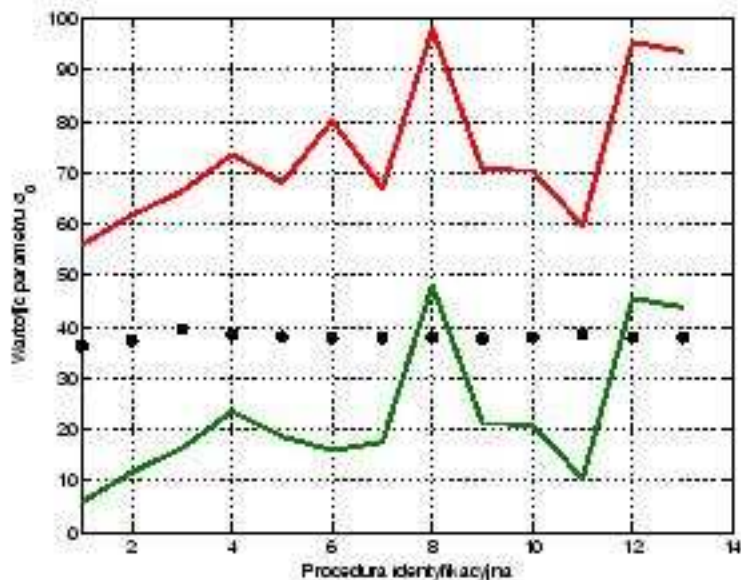


Parameter b obtained on the cluster nodes and initial vector parameter range



Behind the scenes

Example of cluster application

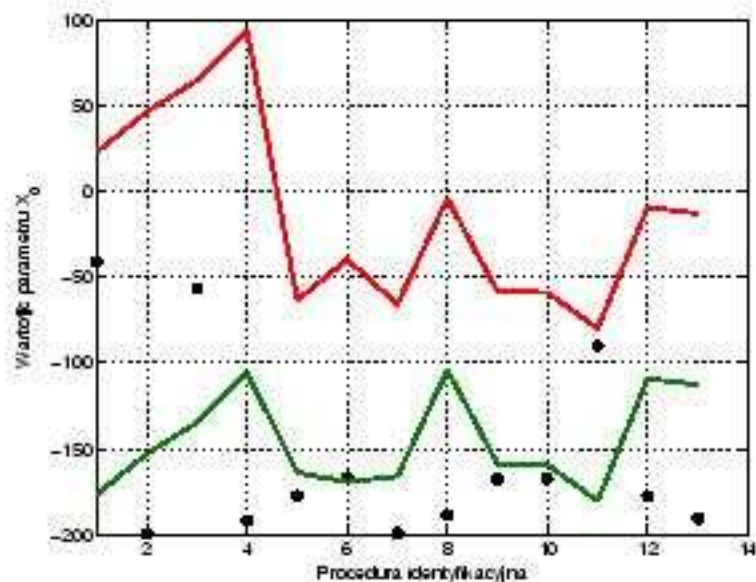


Parameter c obtained on the cluster nodes and initial vector parameter range



Behind the scenes

Example of cluster application

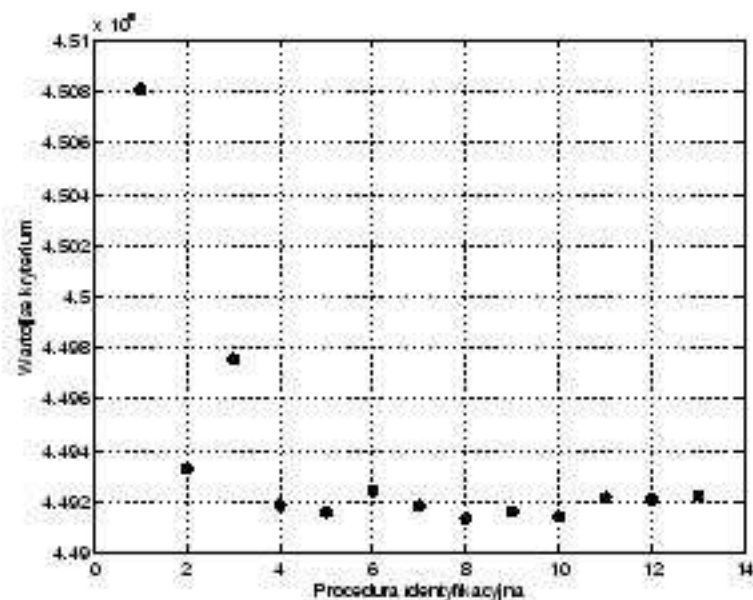


Parameter X_0 obtained on the cluster nodes and initial vector parameter range



Behind the scenes

Example of cluster application



Criterion value computed on the cluster nodes



Behind the scenes

Cluster facts

- ▶ Built upon computers regularly utilised in the Institute's computer laboratory.
- ▶ Consists of virtually the same 17 64-bit AMD Athlon machines (nodes) with 0,5GB RAM installed and over 100GB HDD.
- ▶ The nodes run Debian GNU/Linux operating system, Torque cluster software and Maui queuing application.
- ▶ Approximate total computing power is c.a. 18GFLOPS.



Summary

- ▶ differential evolution algorithm applied to the presented optimisation problem is faster and gives better fits than standard gradient algorithm,
- ▶ cluster computing significantly decreases computation time,
- ▶ the drawback of the presented approach is large amount of data to deal with,
- ▶ the drawback may be partially overcome by keeping clear structure and use of object-oriented programming techniques in optimisation and data manipulation procedures.



Literature

- [1] Maciejewski, Ł., Myszka, W. and Ziętek G.: Estymacja parametrów nieliniowego równania konstytutywnego przy obciążeniach cyklicznych. W: XXI Sympozjum Zmęczenie i Mechanika Pękania, Bydgoszcz 2006
- [2] Storn, R. and Price, K.: Differential Evolution - a Simple and Efficient Adaptive Scheme for Global Optimization over Continuous Spaces. Technical Report TR-95-012, ICSI, March 1995.



Summary

Thank you for your attention!